

94-775/95-865 Lecture 7: Clustering Part III

George Chen

Going from Similarities to Clusters

There's a whole zoo of clustering methods

Two main categories we'll talk about:

Generative models

1. Pretend data generated by specific model with parameters

2. Learn the parameters ("fit model to data")

3. Use fitted model to determine cluster assignments

Hierarchical clustering

Top-down: Start with everything in 1 cluster and decide on how to recursively split

Bottom-up: Start with everything in its own cluster and decide on how to iteratively merge clusters

- 0. Start with everything in the same cluster
 - 1. Use a method to split the cluster

(e.g., *k*-means, with k = 2)

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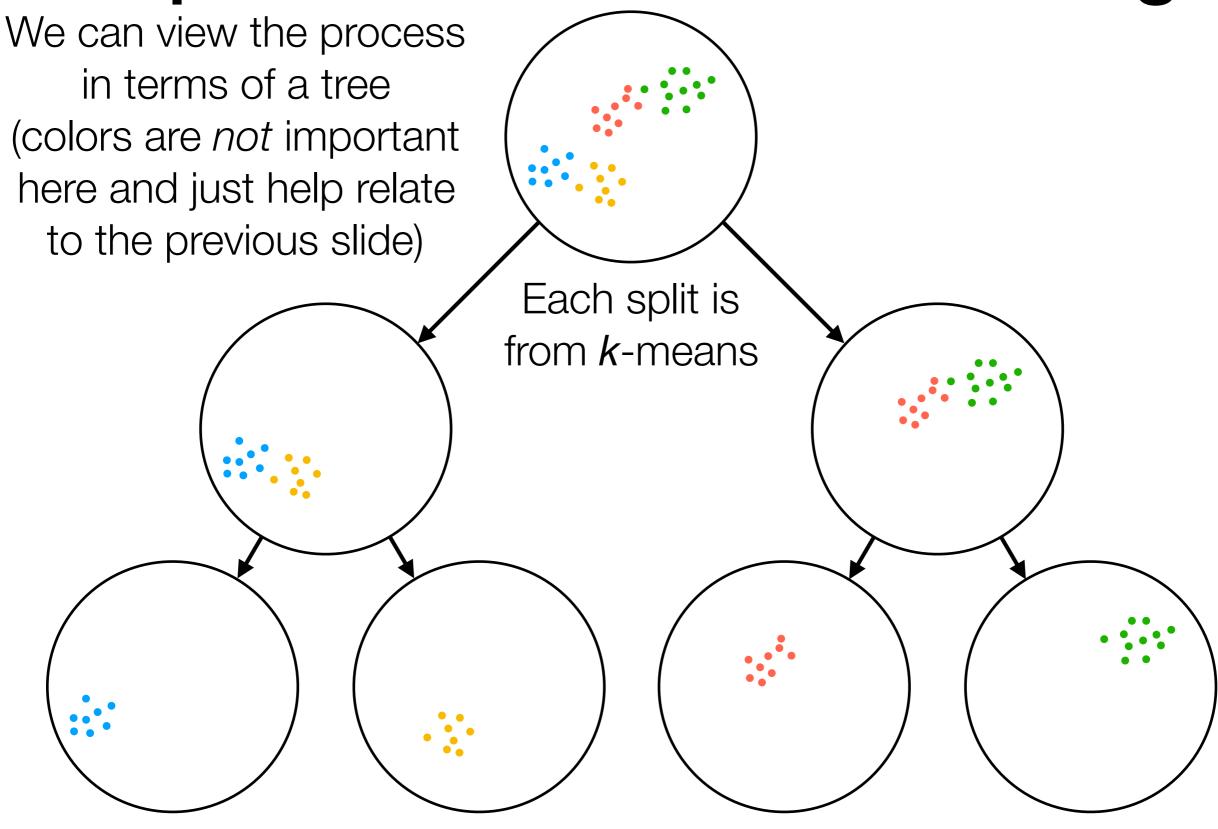
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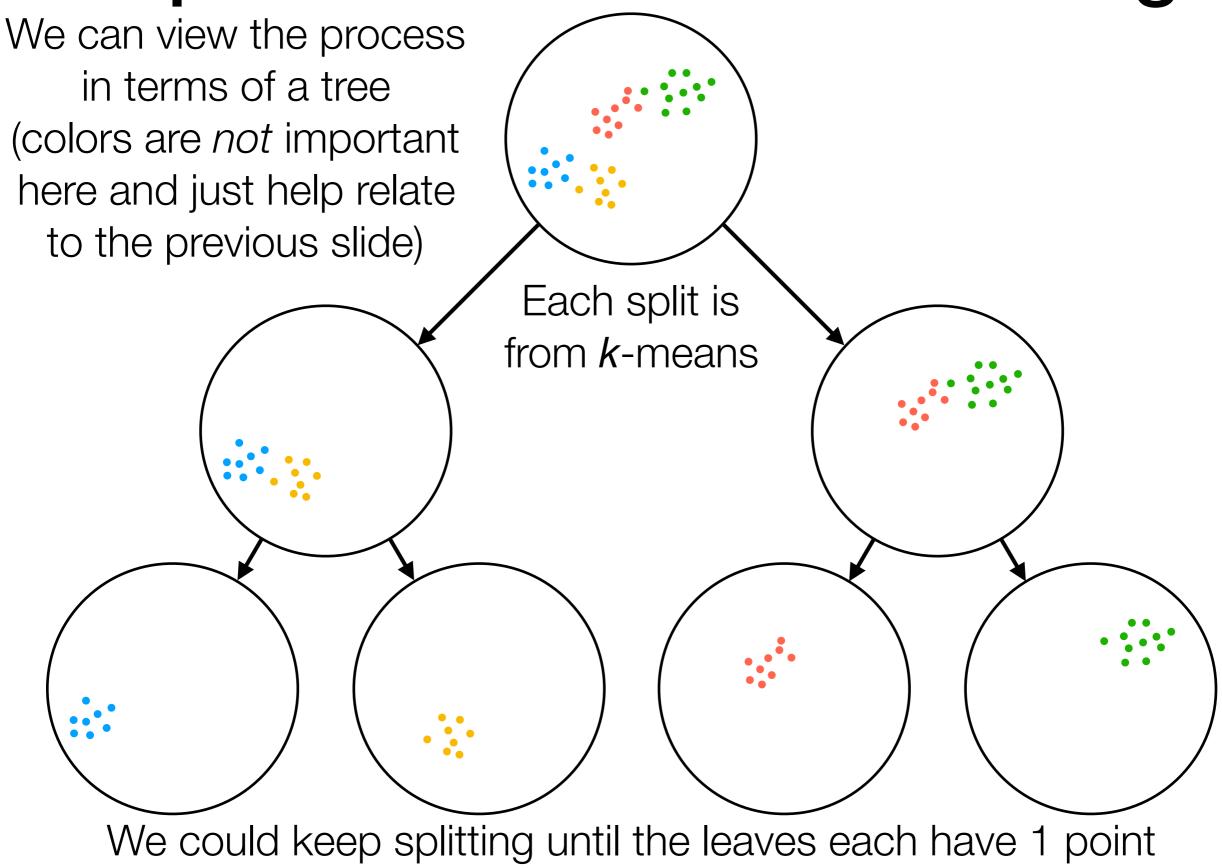
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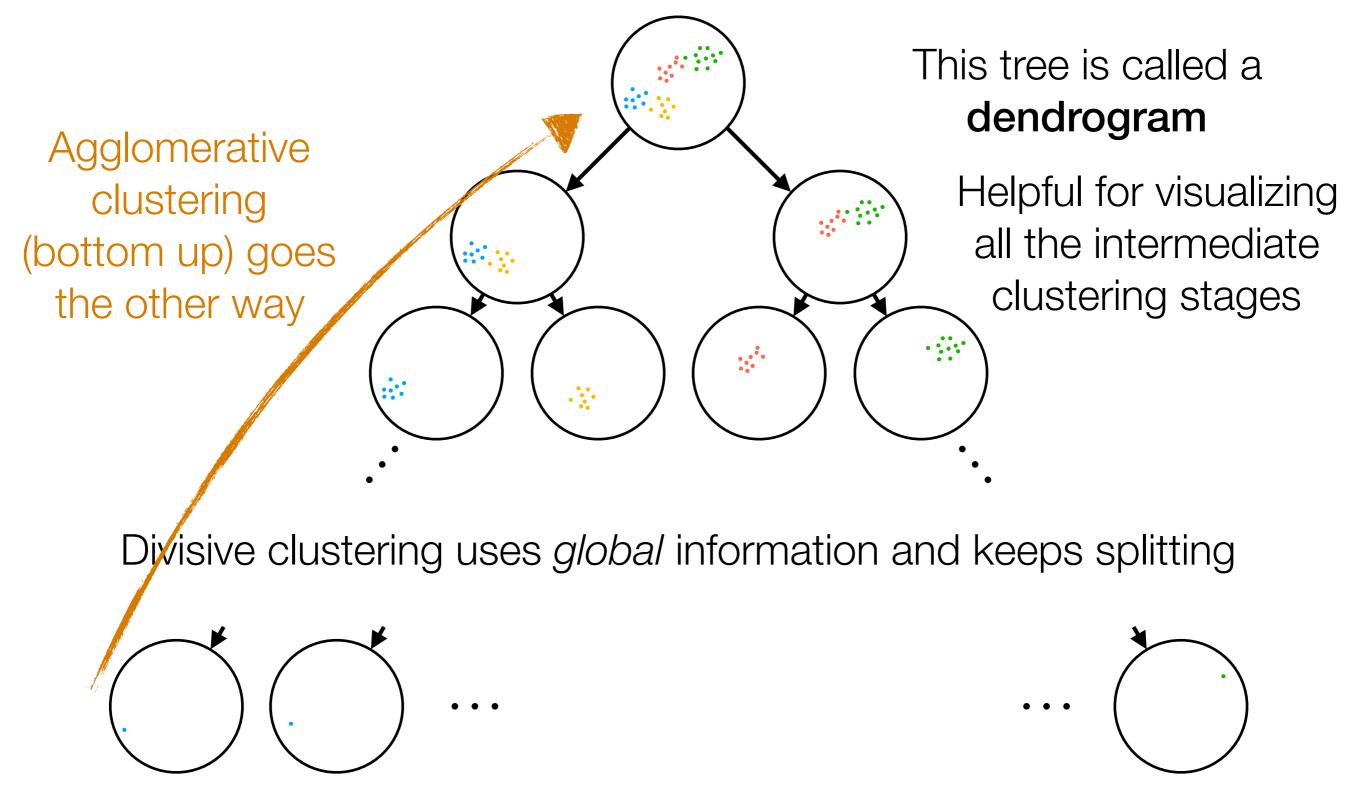
(e.g., *k*-means, with k = 2)

 Decide on next cluster to split
(e.g., pick cluster with highest RSS)

Stop splitting when some termination condition is reached
(e.g., highest cluster RSS is small enough)







We could keep splitting until the leaves each have 1 point

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1. Find the "most similar" two clusters (e.g., pick pair of clusters with closest cluster centers)

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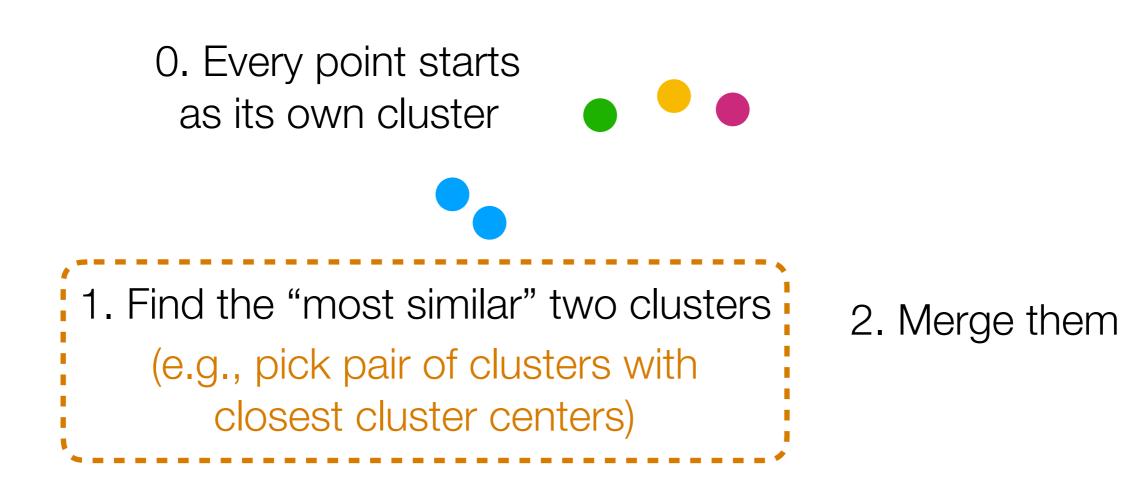
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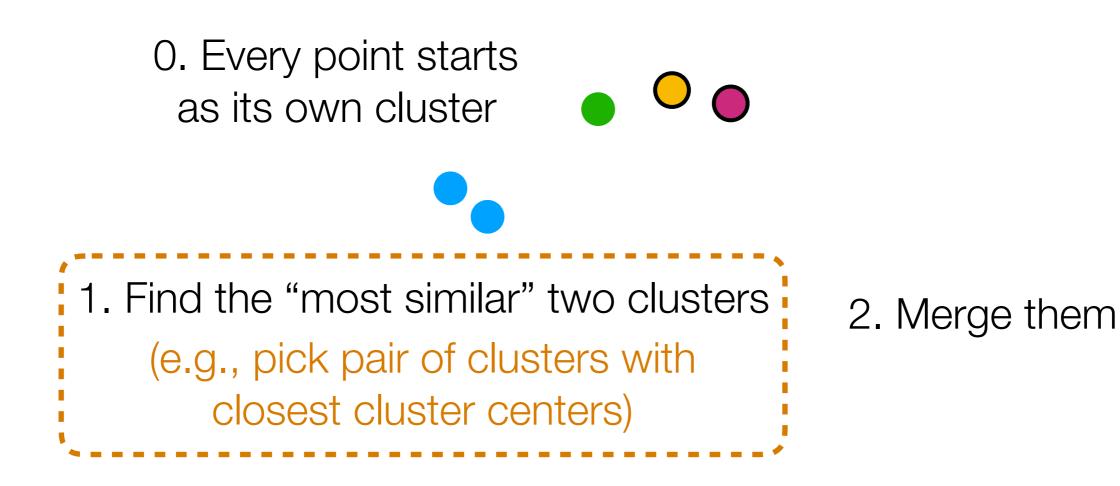
2. Merge them

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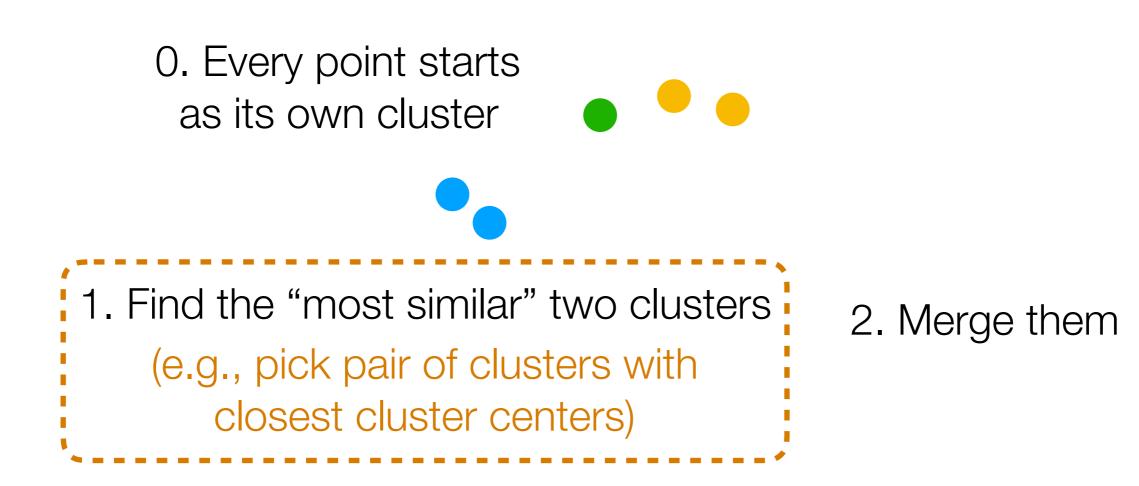
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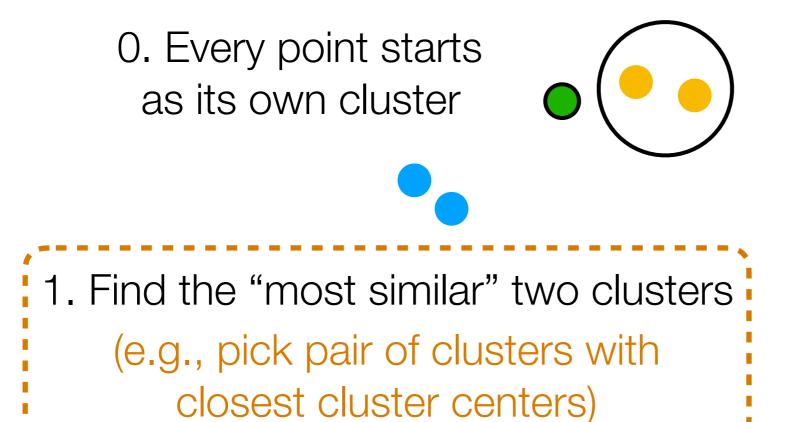


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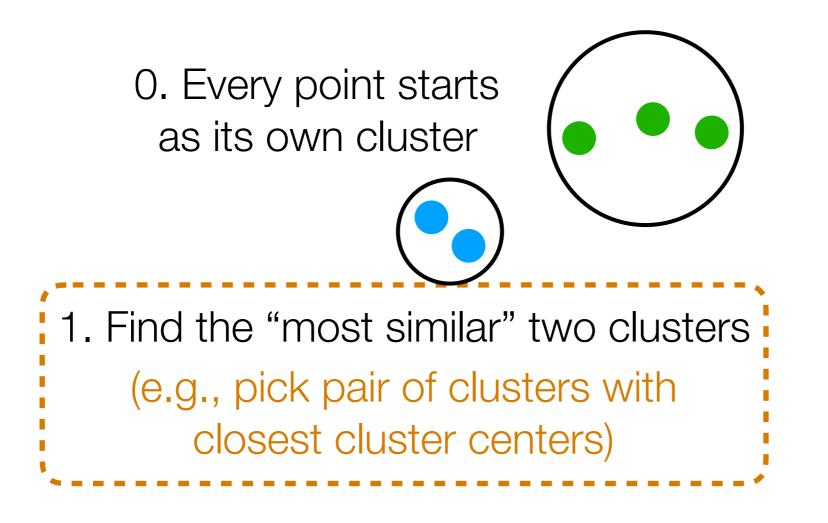
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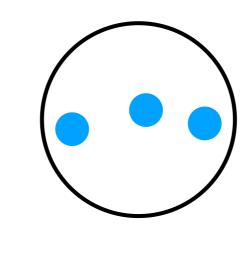
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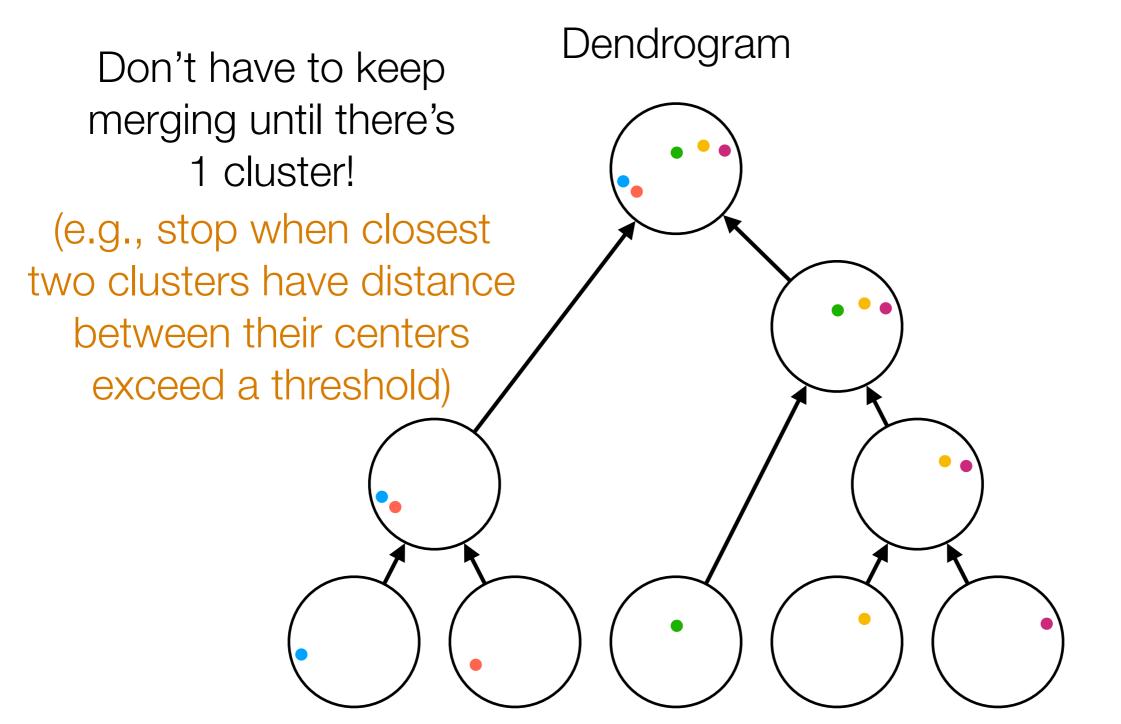
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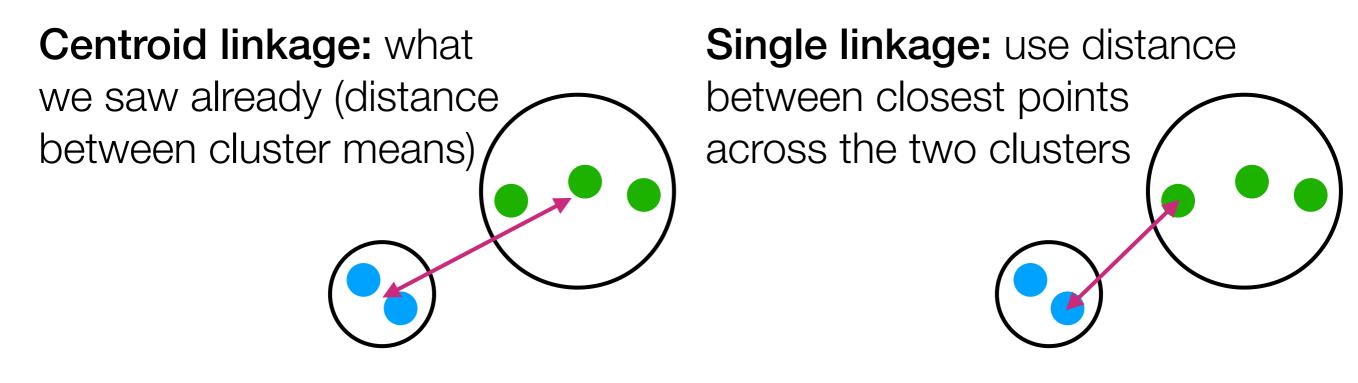
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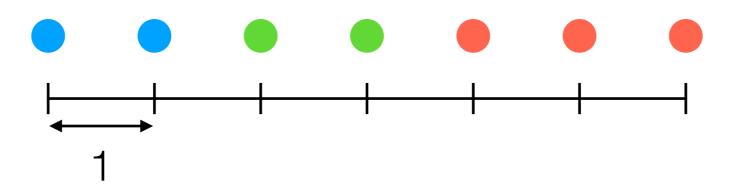


Agglomerative clustering uses local information and keeps merging

Some ways to define what it means for two clusters to be "close" (needed to find most similar clusters):



Example: Single Linkage



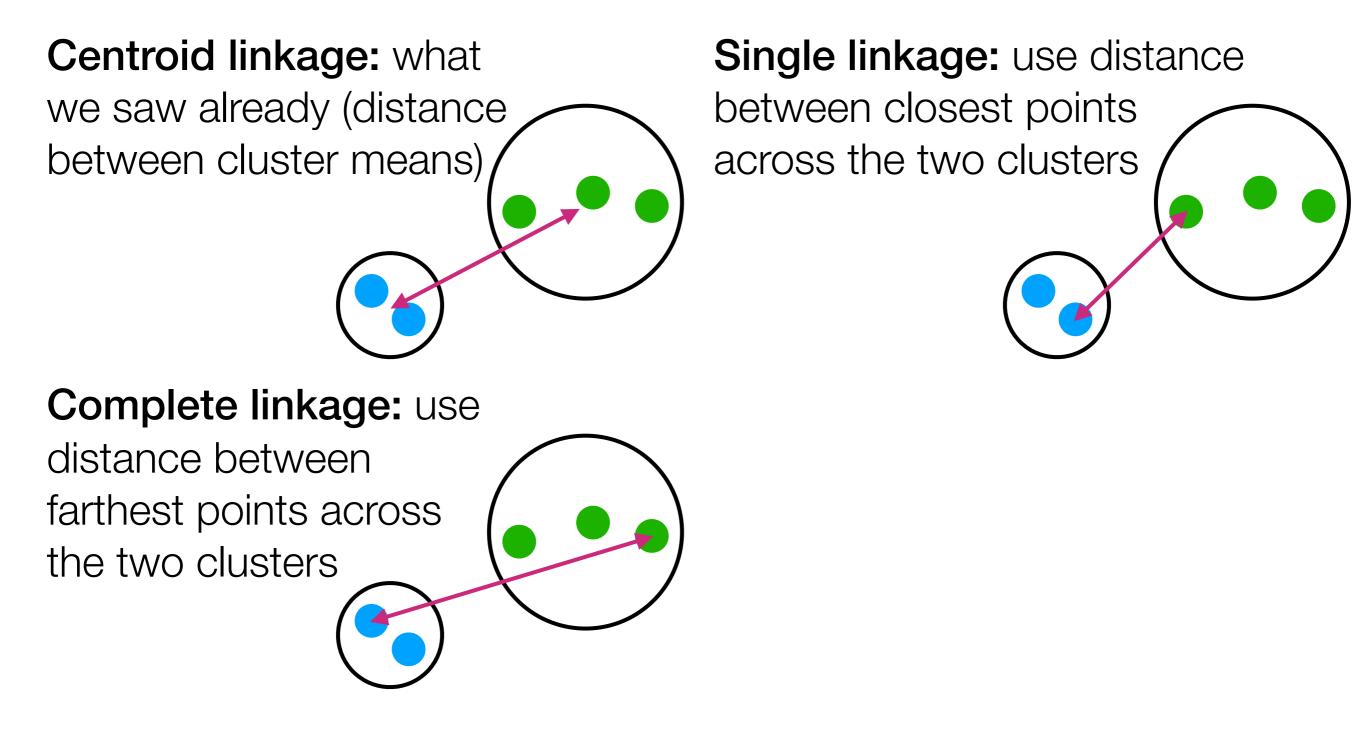
What would single linkage merge next?

Distance between blue and green: 1

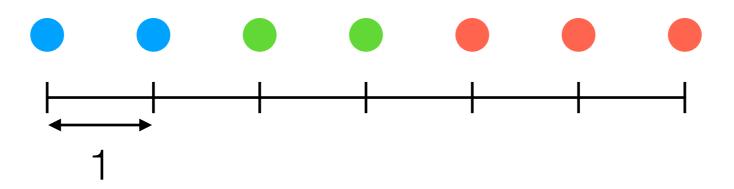
- Distance between blue and red: 3
- Distance between green and red: 1

Single linkage would merge either blue with green, or green with red

Some ways to define what it means for two clusters to be "close" (needed to find most similar clusters):



Example: Complete Linkage

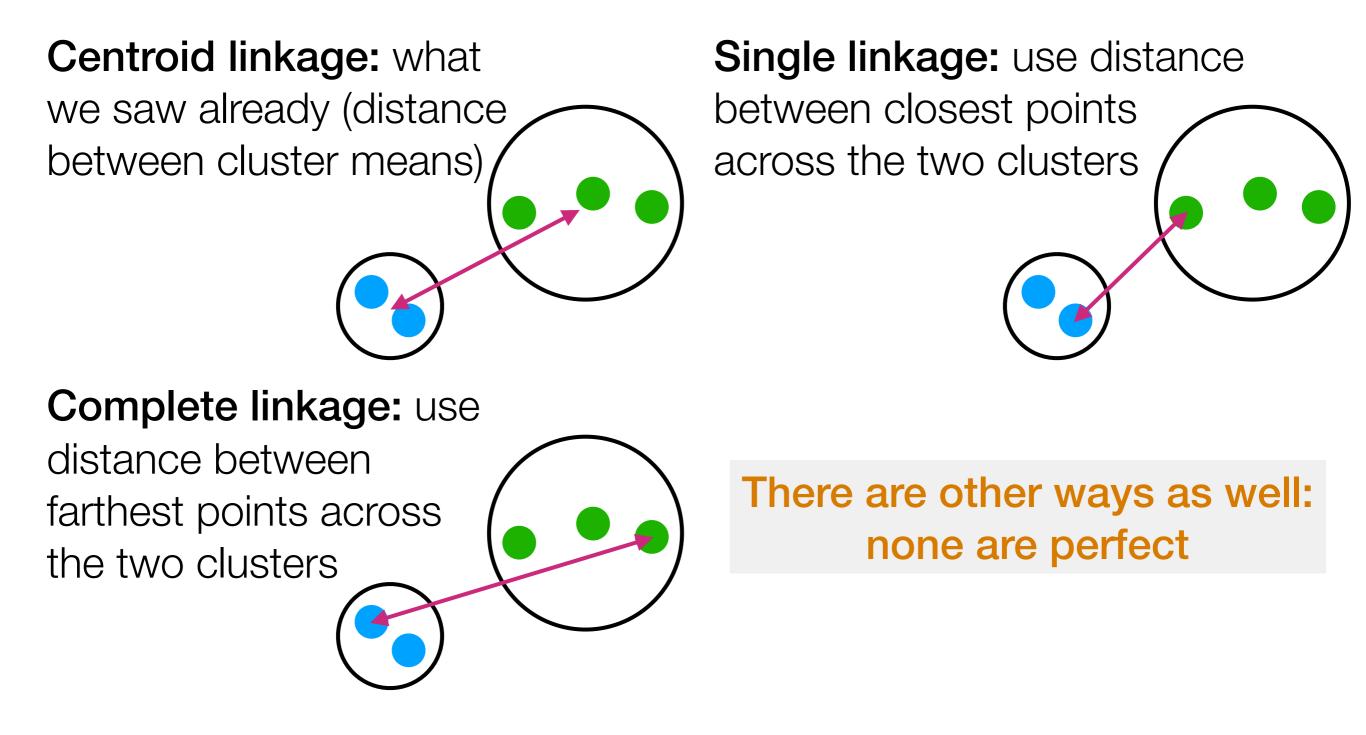


What would complete linkage merge next?

- Distance between blue and green: 3
 - Distance between blue and red: 6
 - Distance between green and red: 4

Complete linkage would merge blue and green

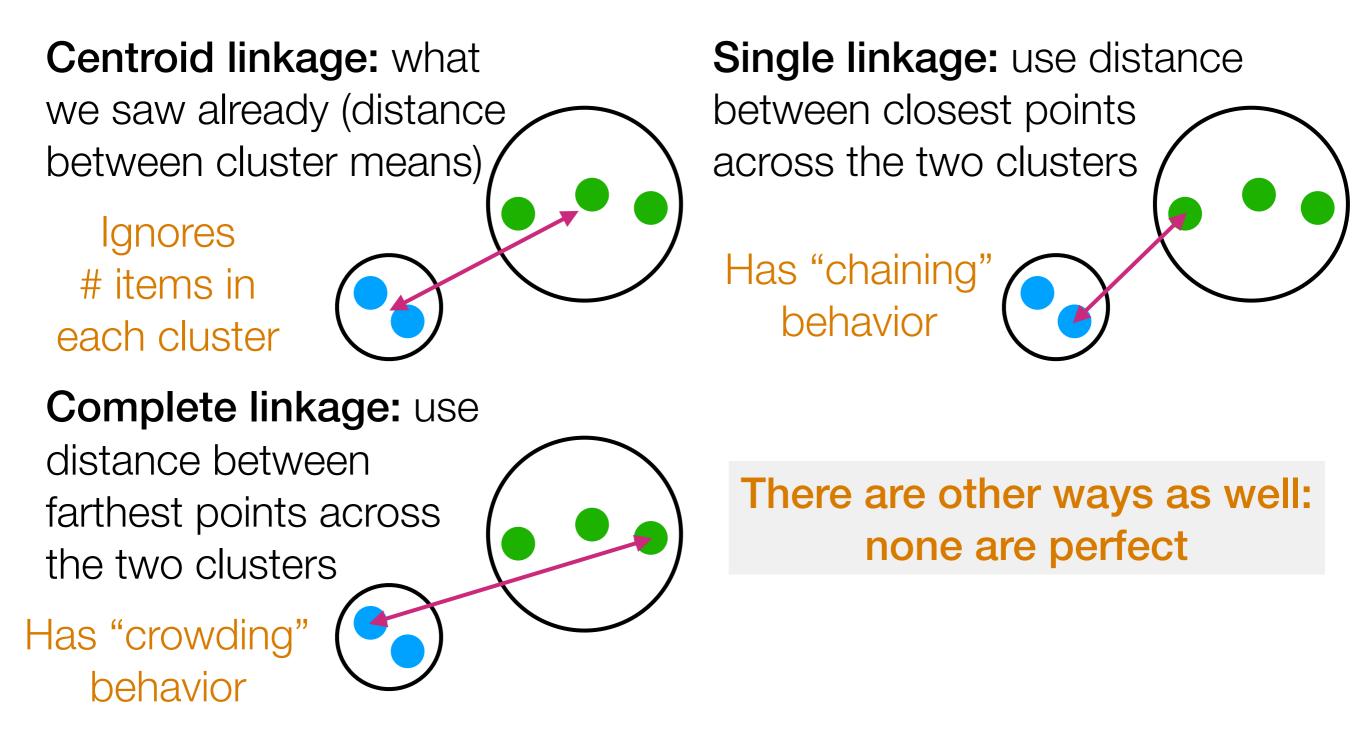
Some ways to define what it means for two clusters to be "close" (needed to find most similar clusters):



Hierarchical Clustering

Demo

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The most popular models effectively assume Euclidean distance...

 You learn a model
→ can predict cluster assignments for points not seen in training

Hierarchical clustering

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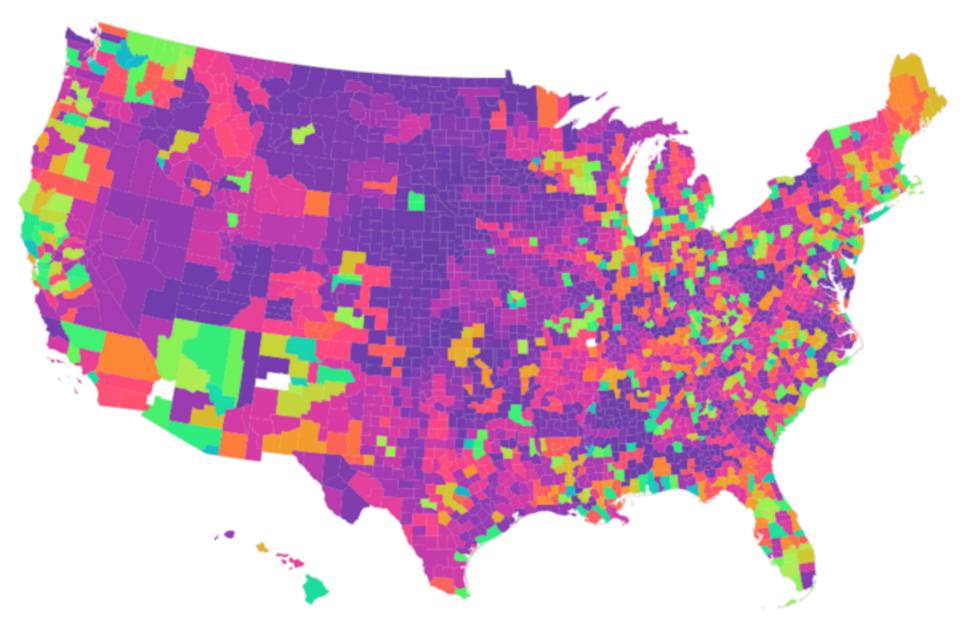
Easily works with different distances (not just Euclidean)

Great for problems that don't need to predict clusters for future points

Different split/merge criteria lead to clusters that look specific ways (e.g., chaining, crowding)

Example: Clustering on U.S. Counties

(using opioid death rate data across 37 years)



No need to predict which cluster new counties should belong to, since we're already looking at all U.S. counties!

Image source: Amanda Coston

How to Choose a Clustering Method?

In general: not easy!

Some questions to think about:

- What features to even cluster on?
- For your application, what distance/similarity makes sense?
- Do you care about cluster assignments for new points?

It's possible that several clustering methods give similar results (*which is great!* — it means that there are some reasonably "stable" clusters in your data)

 Example: tons of clustering methods can figure out from senate voting data who Democrats and Republicans are (of course, without knowing each senator's political party)

Clustering Last Remarks

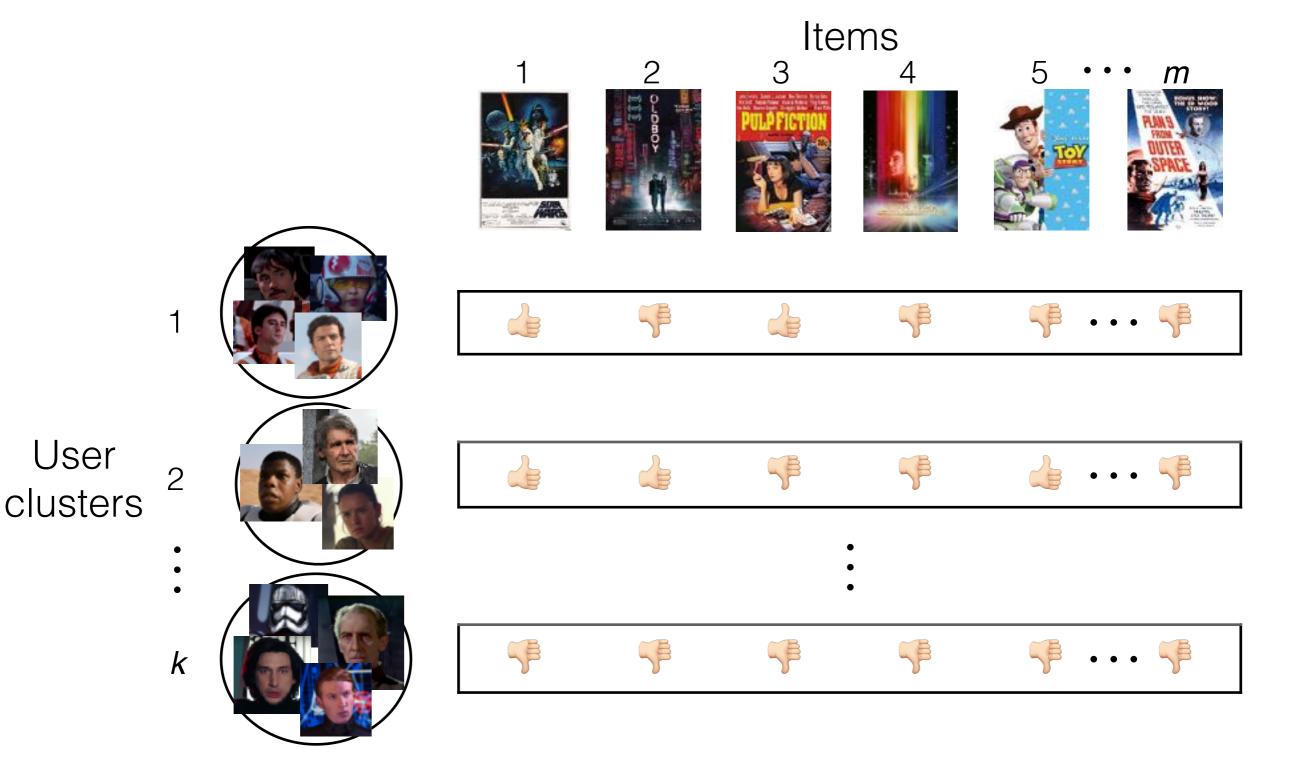
Ultimately, *you* have to decide on which clustering method and number of clusters make sense for your data

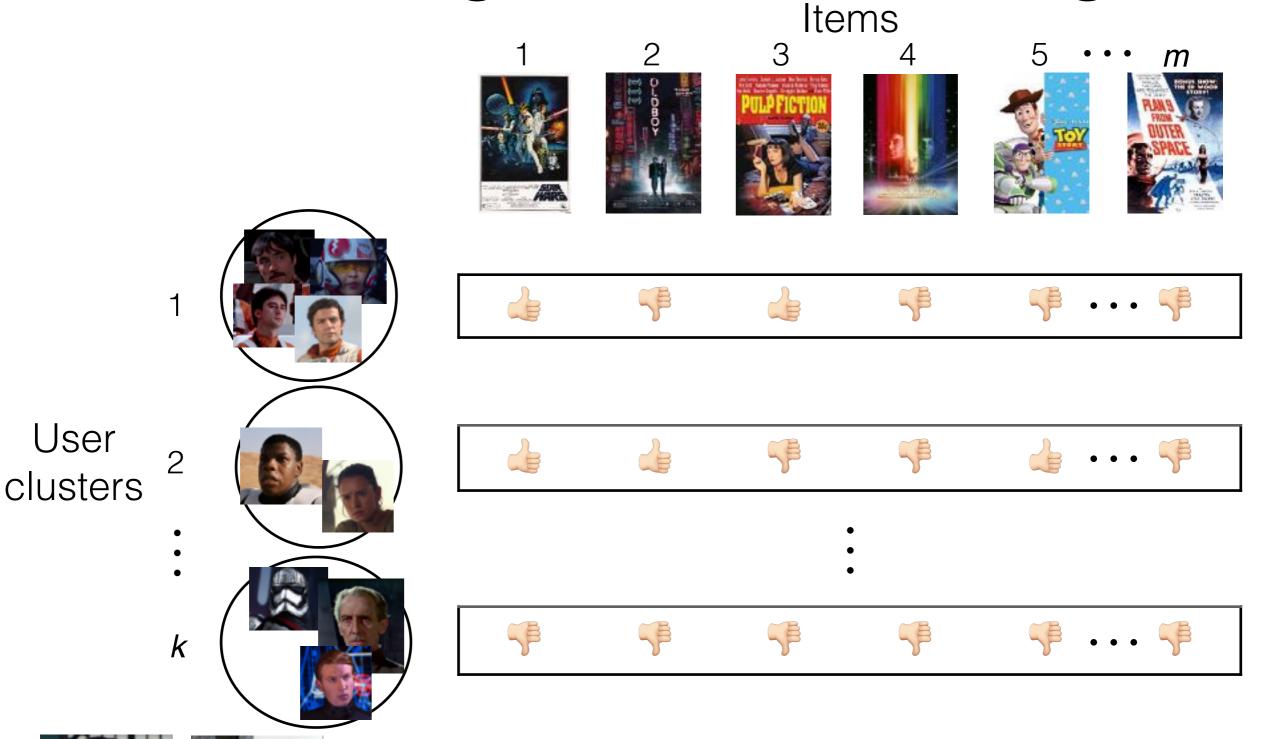
- After you run a clustering algorithm, make visualizations to interpret the clusters *in the context of your application*!
- Do not just blindly rely on numerical metrics (e.g., CH index)
- Some times it makes more sense to define your own score function for how good a clustering assignment is

If you can set up a prediction task, then you can use the prediction task to guide the clustering

User

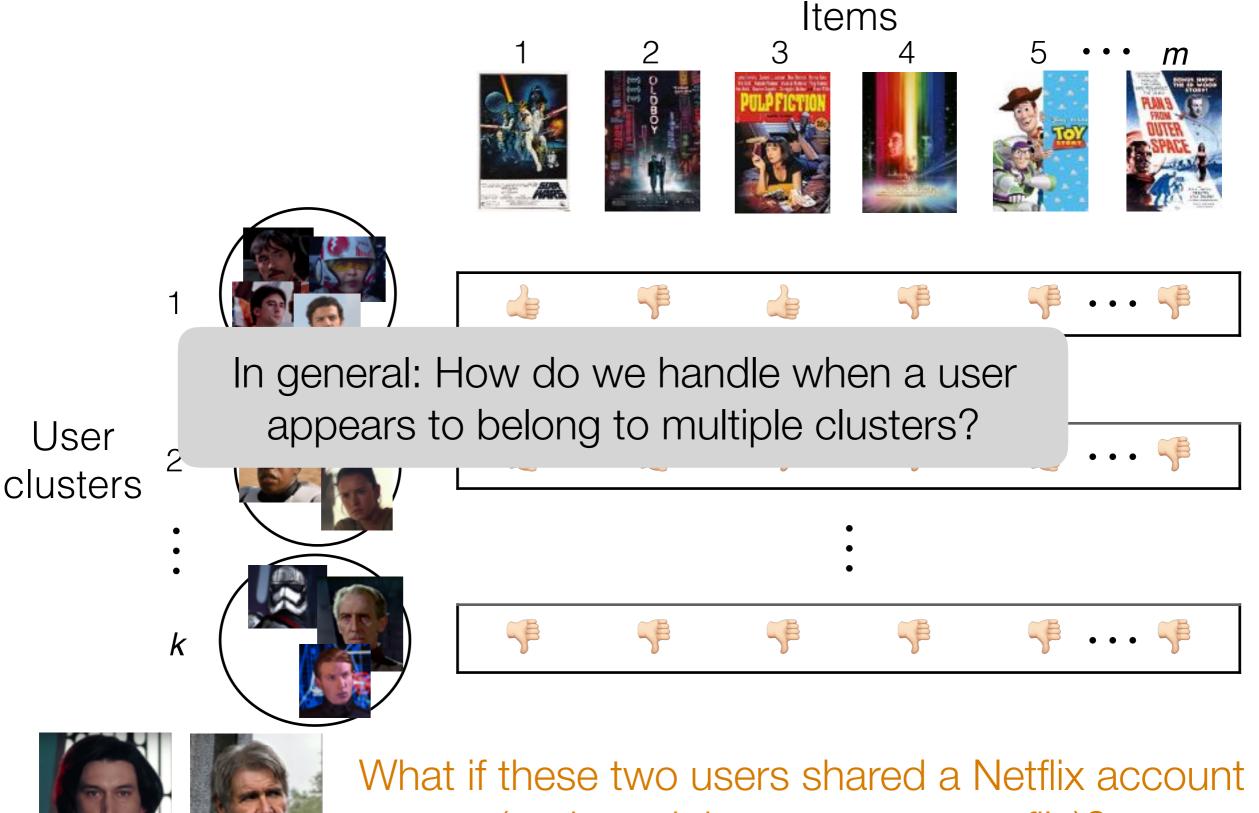








What if these two users shared a Netflix account (and used the same user profile)?



(and used the same user profile)?

Topic Modeling

Movie recommendation

Each user is part of multiple "clusters"/topics

Each cluster/topic consists of a bunch of movies (example clusters: "sci-fi epics", "cheesy rom-coms")

Text

Each document is part of multiple topics

Each topic consists of a bunch of regularly co-occurring words (example topics: "sports", "medicine", "movies", "finance")

Health care

Each patient's health records explained by multiple "topics" Each topic consists of co-occurring "events" (example topics: "heart condition", "severe pancreatitis")

Topic Modeling

Movie recommendation

Each user is part of multiple "clusters"/topics

Each cluster/topic consists of a bunch of movies

(example all lateral "and filables" "abaaav rom aams")

In all of these examples:

- Each data point (a feature vector) is part of multiple topics
- Each to (exar - Each topic corresponds to specific feature words values in the feature vector likely appearing hce")

Health care

Each patient's health records explained by multiple "topics" Each topic consists of co-occurring "events" (example topics: "heart condition", "severe pancreatitis")

Latent Dirichlet Allocation (LDA)

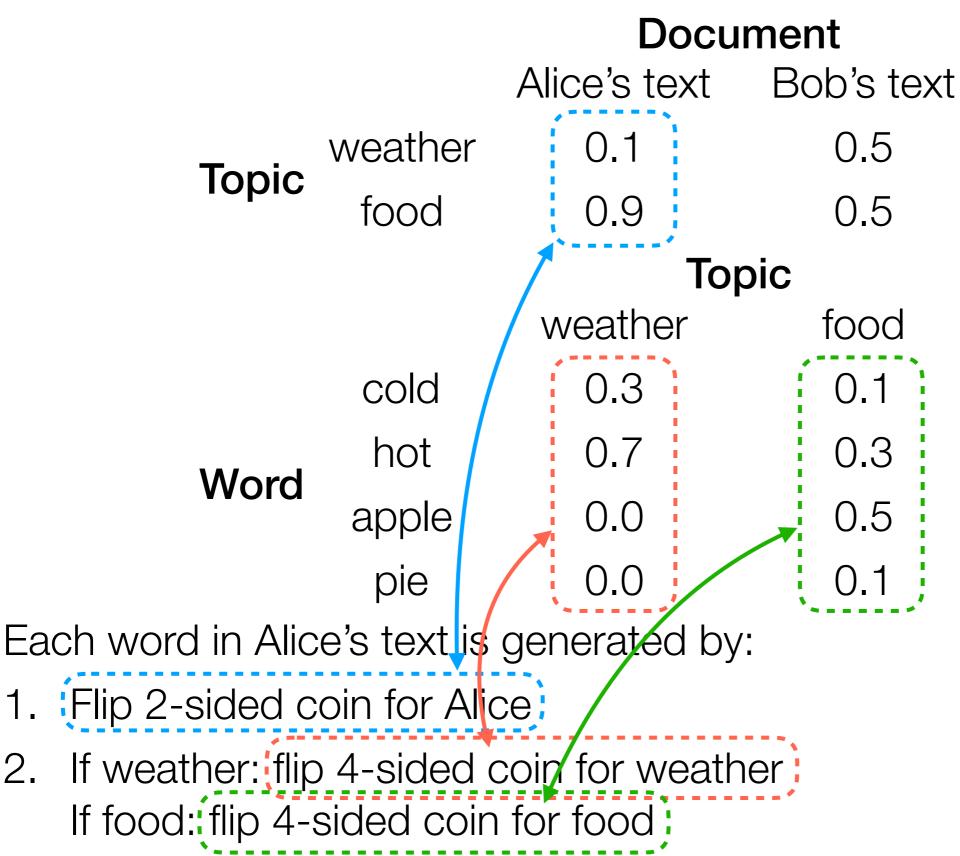
- Easy to describe in terms of text (but works for not just text)
- A generative model
- Input: "document-word" matrix, and pre-specified # topics k



i-th row, *j*-th column: # times word *j* appears in doc *i*

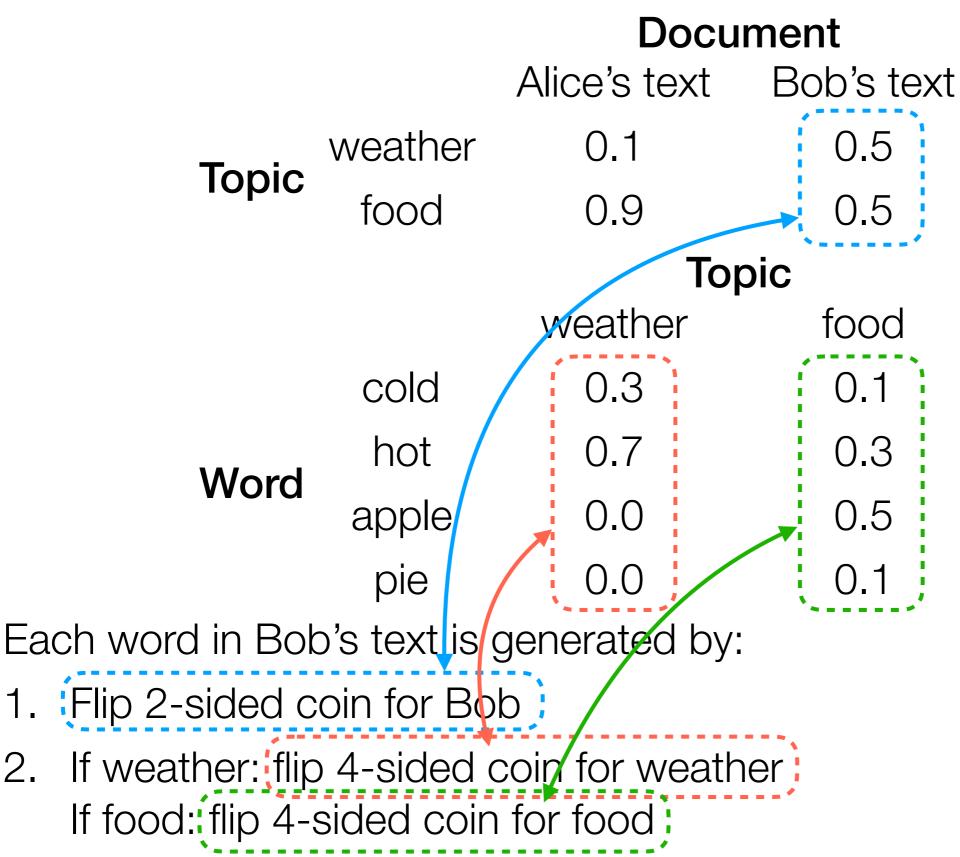
• Output: what the *k* topics are (details on this shortly)

LDA Example



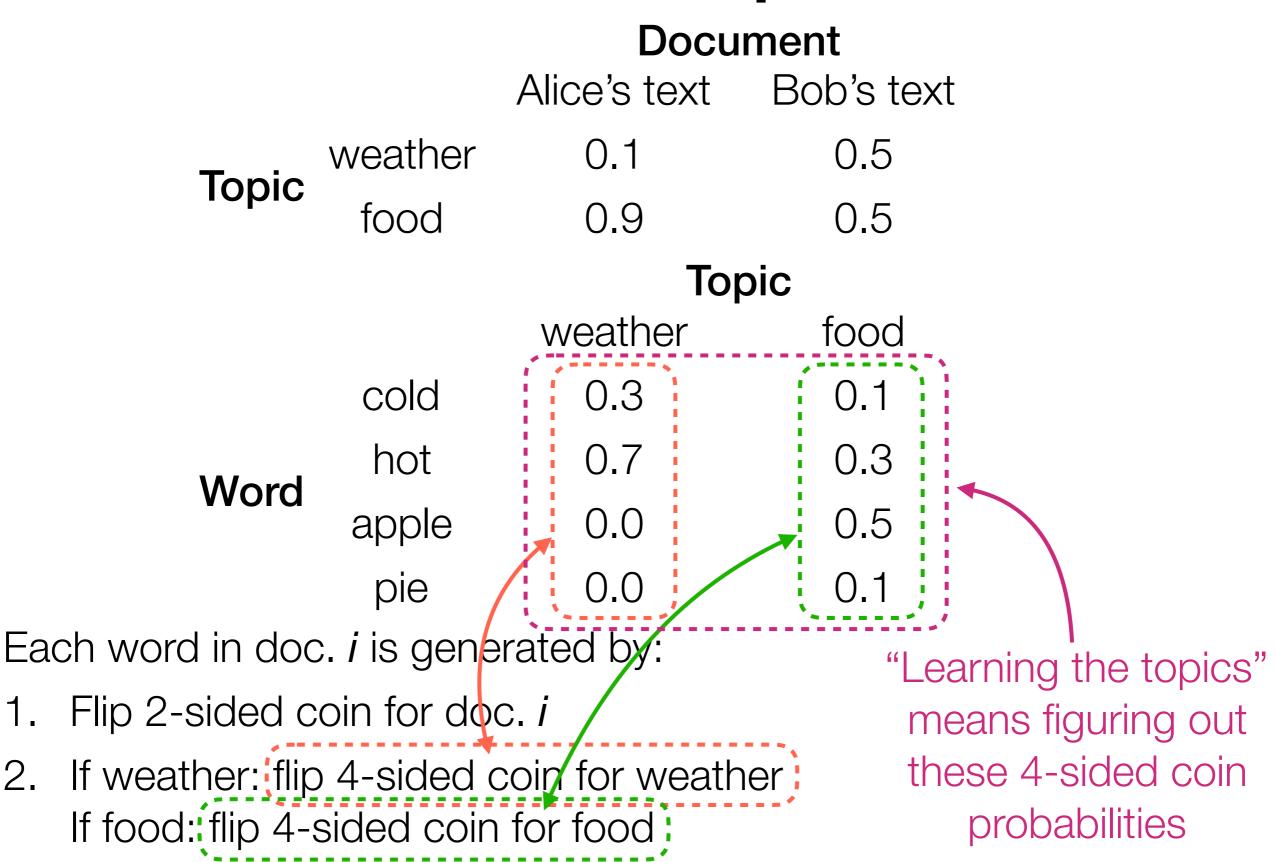
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LDA Example



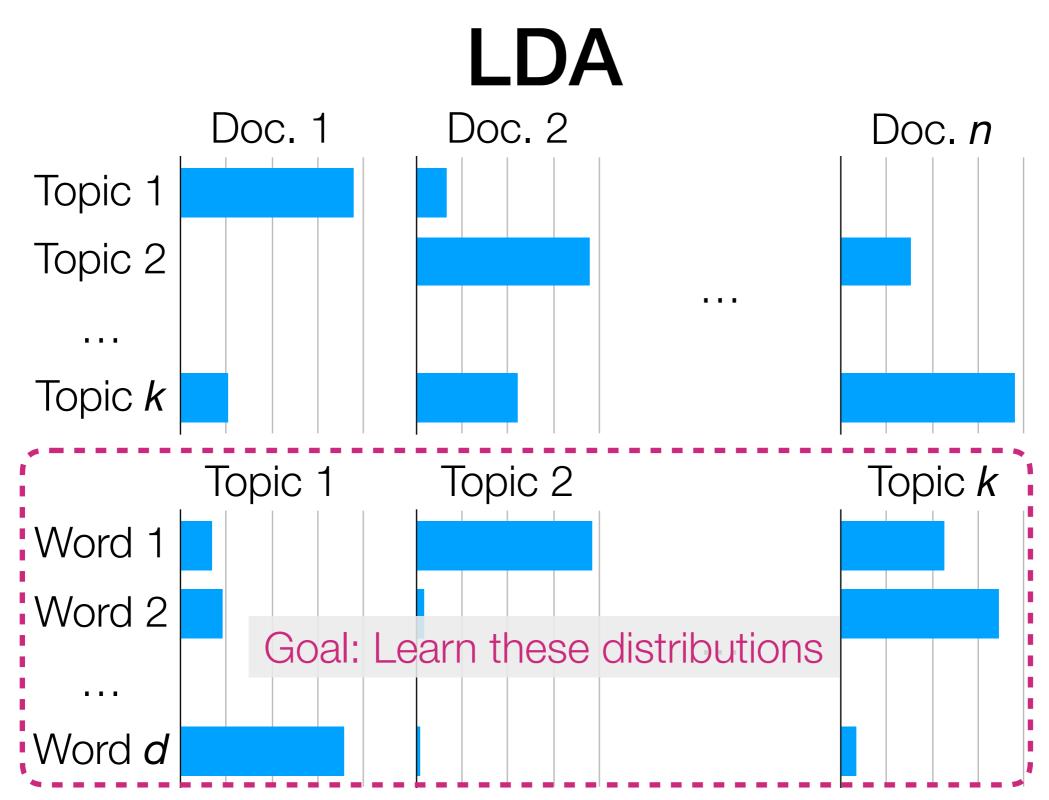
2.

LDA Example



1.

2.



LDA models each word in document *i* to be generated as:

- Randomly choose a topic *Z* (use topic distribution for doc *i*)
- Randomly choose a word (use word distribution for topic Z)

LDA

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i-th row, *j*-th column: # times word *j* appears in doc *i*

• Output: the *k* topics' distribution of words

LDA

Demo